

Function Notation

Functions can be expressed as equations.
For example:

$$y = 3|x - 2| + 7$$

$$y = -\frac{1}{2}\sqrt{x+3} - 4$$

$$y = \frac{1}{x-4} + 5$$

$$y = 2x^2 - 4$$

$$y = 3x^3 - 5$$

We can use function notation to express these exact same functions:

$$f(x) = 3|x - 2| + 7 \quad f(x) = -\frac{1}{2}\sqrt{x+3} - 4 \quad f(x) = \frac{1}{x-4} + 5$$

$$f(x) = 2x^2 - 4$$

$$f(x) = 3x^3 - 5$$

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Function notation is very handy for finding ordered pairs.

Example: $y=3x^2-2$ is the equation.....

Find the value of y if the value of x is -5

$$\begin{aligned} y &= 3(-5)^2 - 2 \\ &= 3(25) - 2 \quad \therefore (-5, 73) \\ &= 75 - 2 \quad \text{is a point} \\ &= 73 \quad \text{on the parabola} \end{aligned}$$

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If we use function notation for the equation

$f(x)=3x^2-2$ is the equation.....

$$\begin{aligned} \text{Find } f(-5) \quad f(-5) &= 3(-5)^2 - 2 \\ &\stackrel{\circ}{=} 3(25) - 2 \\ &= 75 - 2 \\ &= 73 \end{aligned}$$

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Given:

$$f(x) = 2x^2 - 4$$

$$h(x) = -x - 1$$

$$g(x) = \frac{1}{x+2}$$

Example 1

(a) $f(-3)$

(b) $h(-7)$

(c) $g\left(\frac{1}{2}\right)$

$$\begin{aligned} g\left(\frac{1}{2}\right) &= \frac{1}{\frac{1}{2}+2} \quad \therefore \left(\frac{1}{2}, \frac{2}{5}\right) \\ &= \frac{1}{\frac{5}{2}} = \frac{2}{5} \quad \text{is on the curve} \end{aligned}$$

Given:

$$f(x) = 2x^2 - 4$$

$$h(x) = -x - 1$$

$$g(x) = \frac{1}{x+2}$$

Example 2

(a) $f(2x)$

(b) $h(-x+5)$

(c) $g(h(x))$

$$\begin{aligned} \text{(a) } f(2x) &= 2(2x)^2 - 4 \quad \text{b) } h(-x+5) \\ &= 2(4x^2) - 4 \quad = -(-x+5) - 1 \\ &= 8x^2 - 4 \quad = x - 5 - 1 \\ &= x - 6 \end{aligned}$$

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$$\Leftrightarrow g(h(x)) = g(-x-1)$$

$$= \frac{1}{(-x-1)+2}$$

$$= \frac{1}{-x+1}$$

Given:

$$f(x) = 2x^2 - 4$$

$$h(x) = -x - 1$$

$$g(x) = \frac{1}{x+2}$$

Example 3

$$(a) f(x-3)$$

$$(b) h(f(x))$$

$$(c) \quad q(f(-5))$$

$$\begin{aligned}
 (a) \quad & f(x-3) \\
 &= 2(x-3)^2 - 4 \\
 &= 2(x^2 - 6x + 9) - 4 \\
 &= 2x^2 - 12x + 18 - 4 \\
 &= 2x^2 - 12x + 14
 \end{aligned}$$

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$$\begin{aligned}
 b) \quad & h(f(x)) \\
 &= h(2x^2 - 4) \\
 &= -(2x^2 - 4) - 1 \\
 &= -2x^2 + 4 - 1 \\
 &= -2x^2 + 3
 \end{aligned}
 \quad
 \begin{aligned}
 \hookrightarrow \quad & g(f(-5)) \\
 &\underline{\qquad\qquad\qquad} \\
 & f(-5) = 2(-5)^2 - 4 \\
 &= 2(25) - 4 \\
 &= 50 - 4 \\
 &= 46
 \end{aligned}
 \quad
 \begin{aligned}
 \underline{\qquad\qquad\qquad} \\
 & g(46) = \frac{1}{46+2} \\
 &= \frac{1}{48}
 \end{aligned}$$

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