

Write the exponential functions in the form $y = a(b)^x + q$.

Example 1:

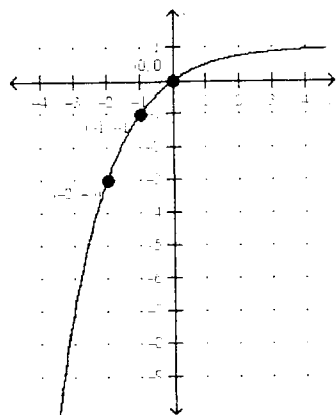
Determine the equation of the exponential function with a common ratio of 3, a y-intercept of 5 and a horizontal asymptote $y = -2$.

Solution:

$$\begin{aligned}
 y &= a(b)^x + q & b = 3 \text{ and } q = -2 \\
 y &= a(3)^x - 2 & \text{sub in pt } (0, 5) \\
 5 &= a(3)^0 - 2 \\
 7 &= a(1) \\
 \therefore a &= 7 \\
 y &= 7(3)^x - 2 \text{ is the equation of the} \\
 &\text{exponential function.}
 \end{aligned}$$

Example 2:

Use the graph to determine the equation of the exponential function.



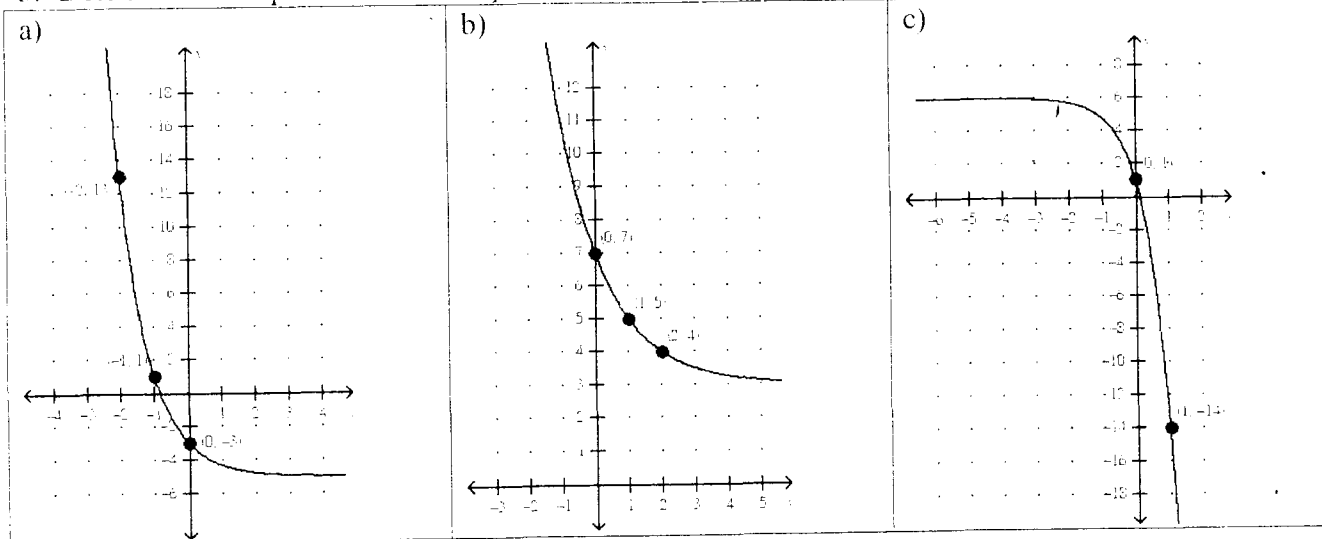
$$\begin{aligned}
 y &= a(b)^x + q \\
 q &= 1
 \end{aligned}$$

Determine common ratio of 1st differences. Sub in a point to get a.

The equation is $y = -\left(\frac{1}{2}\right)^x + 1$.

Exercise:

- Determine the equation of the exponential function with a common ratio of 2, a horizontal asymptote $y = 4$ and passing through the point $(2, 10)$.
- Determine the equation of the exponential function with a common ratio of 3, a horizontal asymptote $y = -4$ and a y-intercept of -6.
- Determine the equations of the exponential functions represented by the graphs below:

**Answers:**

$$\begin{aligned}
 1. & y = 1.5(2)^x + 4 \text{ or } y = 3(2)^{x-1} + 4 & 2. & y = -2(3)^x + 4 & 3. a) & y = 2\left(\frac{1}{3}\right)^x - 5 & b) & y = 4\left(\frac{1}{2}\right)^x + 3 & c) & y = -5(4)^x + 6
 \end{aligned}$$